# Investigation of Induction Motor Drive Behavior in Low-cost Fault Tolerant Control for Electric Vehicles

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Abstract: In this paper, the induction motor drive behavior in a low-cost fault tolerant control system for electric vehicles is investigated. The presented control strategy focuses on the faults of inverter power switches (i.e. short-circuit and open circuit of the inverter legs). The induction motor drive system is based on a voltage source inverter (VSI) controlled with space vector modulation (SVM) algorithm. The presented control system is able to adaptively change-over to different control algorithms when the faults are occurred; also it creates the smooth transitions of the motor current, torque and speed when changing over between the switching algorithms. A 15kW induction motor is used for simulations. The results of the simulations: stator current, electromagnetic torque and speed regulation behaviors demonstrate the performance and validity of the presented fault-tolerant control for induction motor drive fault mitigation.

*Index Terms:* Electrical vehicles, fault tolerant, induction motor, SVM, four-switch inverter.

# 1. Introduction

One of the important issues in electrical vehicle (EV) traction application is electric-propulsion. Electric-propulsion control system has some major requirements that are summarized as follows [1], [2]:

- High instant power and high power density;
- High torque at low speeds for starting and climbing, as well as high power at high speed for cruising;
- Very wide speed range including constant-torque and constant-power regions;
- Fast torque response;
- High efficiency over wide speed and torque ranges;
- High efficiency for regenerative braking;
- High reliability and robustness for various vehicle-operating conditions; and
- Reasonable cost.

Proper operation of this control system depends on the reliable performance of electric-motor, three-phase inverter and control and instrumentation circuitry. Each of these sections may have a fault in their operations that are summarized as follows [3]:

Electric-motor faults include:

Single phase failure

- Multi-phase failure
- Eccentricity
- Demagnetization

Three-phase inverter faults include:

- Component failure
- Single leg failure
- Multiple leg failure
- Failure in gate drivers
- Failure in interface

And control and instrumentation circuitry faults include:

- Failure of position encoder
- Failure of sensorless control
- Failure of current sensor
- Failure of filter and signal conditioning circuit

Several failures can affect electrical-motor drives, and

many different treatment methods have been proposed [4]-[8]. Therefore, redundant or conservative design has been used to robust continuity operation in a reasonable state when the faults are occurred. Some of these designs may have short torque transients and even reduced drive performance after a fault, on the condition that the drive still goes running. This is especially important in EV electrical-motor drives that should have high reliability and robustness for various vehicle-operation conditions. This paper describes a low-cost fault tolerant control system in induction motor drive for EV. The presented control strategy focuses on the faults of inverter power switch (i.e. short-circuit and open circuit of the inverter legs). Many different control strategies and circuit topologies have been proposed to provide fault tolerant capabilities under the conditions [6],[8]-[13]. The presented control strategy runs closed-loop conventional SVM algorithm for six-switch inverter topology with extra switches that will be used by fault tolerant control (Figure 1). When one of the inverter legs is lost (the short-circuit leg is disconnected by fuse, also it will be such as an open circuit), it change-overs to a closed-loop modified SVM algorithm for four-switch inverter topology by one of the extra switches (Figure 2), and it connects the stator winding that lost the third leg of sixswitch inverter, to the middle point of a capacitor bank. In the following sections the equations of conventional SVM algorithm for six-switch inverter topology and the

modified SVM algorithm for four-switch inverter topology is derived. Then the simulation procedures and results: stator current, electromagnetic torque and speed regulation behaviors are shown. and Table 1. Vectorial voltages are done by using equation 8.



Figure 1 Six-switch inverter topology with extra switches



Figure 2 Four-switch inverter topology

# 2. Space Vector Modulation

The switching status of circuit in Figure 1 and Figure 2 is represented by the binary variables  $S_1$  to  $S_6$  and  $S_1$  to  $S_4$  respectively, which values of '1' and '0' indicate closed and open switch respectively. In addition, the switches of each leg are controlled complementary (i.e.  $S_2 = 1 - S_1$ ). In the following phase voltages, vector voltages and switching time calculation are derived (Z is negative pole of battery and N is neutral point of motor).

### 2.1 Six-Switch Inverter Algorithm

Pole voltages of motor in Figure 1 are determined by the switching status can be obtained as:

$$V_{AZ} = S_1 \cdot V_{bat} \tag{1}$$

$$V_{BZ} = S_3 \cdot V_{bat} \tag{2}$$

$$V_{CZ} = S_5 \cdot V_{bat} \tag{3}$$

And:

$$V_{NZ} = 1/3 \left( V_{AZ} + V_{BZ} + V_{CZ} \right)$$
(4)

Therefore, phase voltages can be written as:

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$$V_{AN} = V_{AZ} - V_{NZ} \tag{5}$$

$$V_{BN} = V_{BZ} - V_{NZ} \tag{6}$$

$$V_{CN} = V_{CZ} - V_{NZ} \tag{7}$$

Combinations of switching  $S_1$  to  $S_6$  produce six different space vector voltages that are shown in Figure 3







Table 1.Vectorial voltages in six-switch inverter					
Vector	On Switch	V <sub>AZ</sub>	V <sub>BZ</sub>	V <sub>cz</sub>	$\vec{v}_{lphaeta}$
$\vec{v}_{o}$	S <sub>2</sub> S <sub>4</sub> S <sub>6</sub>	0	0	0	ō
$\vec{v}_1$	S <sub>1</sub> S <sub>4</sub> S <sub>6</sub>	V <sub>bat</sub>	0	0	$\frac{2V_{bat}}{3}e^{j0}$
$\vec{v}_{z}$	S <sub>1</sub> S <sub>3</sub> S <sub>6</sub>	V <sub>bat</sub>	V <sub>bat</sub>	0	$\frac{2V_{bat}}{3}e^{j\frac{\pi}{3}}$
$\vec{V}_3$	S <sub>2</sub> S <sub>3</sub> S <sub>6</sub>	0	V <sub>bat</sub>	0	$\frac{2V_{bat}}{3}e^{j\frac{2\pi}{3}}$
<b>V</b> 4	S <sub>2</sub> S <sub>3</sub> S <sub>5</sub>	0	V <sub>bat</sub>	V <sub>bat</sub>	$\frac{2V_{bat}}{3}e^{j\pi}$
$\vec{V}_5$	S <sub>2</sub> S <sub>4</sub> S <sub>5</sub>	0	0	V <sub>bat</sub>	$\frac{2V_{bat}}{3}e^{j\frac{-2\pi}{3}}$
$\vec{V}_6$	S <sub>1</sub> S <sub>4</sub> S <sub>5</sub>	$\frac{2V_{bat}}{3}$	0	V <sub>bat</sub>	$\frac{2V_{bat}}{3}e^{j\frac{-\pi}{3}}$
<b>V</b> 7	S <sub>1</sub> S <sub>3</sub> S <sub>5</sub>	V <sub>bat</sub>	V <sub>bat</sub>	V <sub>bat</sub>	ō

Each desired position on circular for the vector voltage  $V_S$ in Figure 3 can be achieved by a time average relationship between two neighbouring active vectors  $(t_a \& t_b)$ . Zero state vectors  $(t_0)$  are used to fill up the gap to a constant sampling interval  $T_S$ . To calculate  $t_a \& t_b \& t_0$ , decomposition  $V_S$  along Real and Imaginary axes in Figure 3:

$$\vec{V}_{S}T_{S} = \vec{V}_{1}t_{a} + \vec{V}_{2}t_{b} + \vec{V}_{0}\frac{t_{0}}{2} + \vec{V}_{7}\frac{t_{0}}{2}$$
(9)

$$T_s = t_a + t_b + t_0 \tag{10}$$

Real: 
$$V_S \cdot \cos \varphi \cdot T_S = \frac{2V_{bat}}{3} \cdot 1 \cdot t_a + \frac{2V_{bat}}{3} \cdot \frac{1}{2} \cdot t_b$$
 (11)

Imag: 
$$V_S \cdot \sin \varphi \cdot T_S = \frac{2V_{bat}}{3} \cdot 0 \cdot t_a + \frac{2V_{bat}}{3} \cdot \frac{\sqrt{3}}{2} \cdot t_b$$
 (12)

With the solution:

$$t_a = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( \nu_x - \frac{1}{\sqrt{3}} \cdot \nu_y \right) \tag{13}$$

$$t_b = \frac{\sqrt{3} \cdot T_S}{V_{bat}} \left( v_y \right) \tag{14}$$

$$t_0 = T_S - t_a - t_b \tag{15}$$

That  $v_x = V_S \cdot \cos \varphi$ ,  $v_v = V_S \cdot \sin \varphi$ .

 $t_a \& t_b$  in all sectors are shown in Table 2:

Sec1	$t_a = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( v_x - \frac{1}{\sqrt{3}} \cdot v_y \right)$	$t_b = \frac{\sqrt{3} \cdot T_S}{V_{bat}} (v_y)$
Sec2	$t_a = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( v_x + \frac{1}{\sqrt{3}} \cdot v_y \right)$	$t_b = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( -v_x + \frac{1}{\sqrt{3}} \cdot v_y \right)$
Sec3	$t_a = \frac{\sqrt{3} \cdot T_s}{V_{bat}} (v_y)$	$t_b = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( -v_x - \frac{1}{\sqrt{3}} \cdot v_y \right)$
Sec4	$t_a = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( -v_x + \frac{1}{\sqrt{3}} \cdot v_y \right)$	$t_b = \frac{-\sqrt{3} \cdot T_s}{V_{bat}} (v_y)$
Sec5	$t_a = \frac{3 \cdot T_S}{2 \cdot V_{bat}} \left( -v_x - \frac{1}{\sqrt{3}} \cdot v_y \right)$	$t_b = \frac{3 \cdot T_s}{2 \cdot V_{bat}} \left( v_x - \frac{1}{\sqrt{3}} \cdot v_y \right)$
Sec6	$t_a = \frac{-\sqrt{3} \cdot T_S}{V_{bat}} (v_y)$	$t_b = \frac{3 \cdot T_s}{2 \cdot V_{bat}} \left( v_x + \frac{1}{\sqrt{3}} \cdot v_y \right)$

### Table 2. Switching time in each sector

#### 2.2 **Four-Switch Inverter Algorithm**

Pole voltages of motor in Figure 2 are determined by the switching status can be obtained as:

$$V_{AZ} = S_1 \cdot V_{bat} \tag{16}$$

$$V_{BZ} = S_3 \cdot V_{bat}$$
(17)  
$$V_{CZ} = V_{bat}/2$$
(18)

$$V_{CZ} = V_{bat}/2 \tag{1}$$

And:

$$V_{NZ} = 1/3 \left( V_{AZ} + V_{BZ} + V_{CZ} \right)$$
(19)

Therefore, phase voltages can be written as:

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$$V_{AN} = V_{AZ} - V_{NZ} \tag{20}$$

$$V_{BN} = V_{BZ} - V_{NZ} \tag{21}$$

$$V_{CN} = V_{CZ} - V_{NZ} \tag{22}$$

Like six-switch inverter, combinations of switching  $S_1$ to  $S_4$  produce four different space vector voltages that are shown in Figure 4 and Table 3. Vector voltages are done by using equation 8.



Figure 4.Space vector voltages of different switching status in fourswitch inverter [8]

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Vector	On Switch	V <sub>AZ</sub>	V <sub>BZ</sub>	V <sub>cz</sub>	$ec{v}_{lphaeta}$
<i>V</i> <sub>1</sub>	<i>S</i> <sub>2</sub> <i>S</i> <sub>4</sub>	0	0	$V_{bat}/2$	$\frac{V_{bat}}{3} \cdot e^{-j\frac{2\pi}{3}}$
$\vec{v}_2$	<i>S</i> <sub>1</sub> <i>S</i> <sub>4</sub>	V <sub>bat</sub>	0	$V_{bat}/2$	$\frac{\sqrt{3}V_{bat}}{3} \cdot e^{-j\frac{\pi}{6}}$
$\vec{V}_3$	<i>S</i> <sub>1</sub> <i>S</i> <sub>3</sub>	V <sub>bat</sub>	V <sub>bat</sub>	$V_{bat}/2$	$\frac{V_{bat}}{3} \cdot e^{j\frac{\pi}{3}}$
<b>V</b> 4	<i>S</i> <sub>2</sub> <i>S</i> <sub>3</sub>	0	V <sub>bat</sub>	$V_{bat}/2$	$\frac{\sqrt{3}V_{bat}}{2} \cdot e^{j\frac{5\pi}{6}}$

Table 3. Vector voltages in four-switch inverter

As it can be seen in Table 3, four-switch inverter has no zero vectors. This means that in order to fill up the gap to a constant sampling interval  $T_S$ , modified SVM algorithm should be developed based on the remaining active vectors (Figure 4). The switching time equation is:

$$\vec{V}_{S}T_{S} = \vec{V}_{1}t_{1} + \vec{V}_{2}t_{2} + \vec{V}_{3}t_{3} + \vec{V}_{4}t_{4}$$
(23)

The opposite vectors  $V_1 \& V_3$  or  $V_2 \& V_4$  can be used to make zero vector to fill up the gap. Only three of four vectors are required to accurately define the magnitude and the phase of  $\vec{V}_{S}$  during the switch period  $T_{S}$ . There are two possibilities to select three vectors. It is better to select two short and one leg vectors instead of two long and one short; because the long vectors make larger voltage drop on inductive loads and larger ripple. So on that, there are two groups of three vectors; one group include the long vector  $\vec{V}_2$  and the other group include the long vector  $\vec{V}_4$ . So to derive SVM timings there are two groups of adjacent sectors in vector space.

Sector 1 and 2 (
$$-\frac{2\pi}{2} < \varphi < \frac{\pi}{2}$$

The switching time equation is:

$$\vec{V}_{S}T_{S} = \vec{V}_{1}t_{1} + \vec{V}_{2}t_{2} + \vec{V}_{3}t_{3}$$
(24)

The vector decomposition of the above equation along Real and Imaginary axes in Figure 4:

$$T_S = t_1 + t_2 + t_3 \tag{25}$$

Real: 
$$V_S T_S \cos \varphi = -V_1 t_1 \cos \frac{\pi}{3} + V_2 t_2 \cos \frac{\pi}{6} + V_3 t_3 \cos \frac{\pi}{3}$$
 (26)

*Imag*: 
$$V_{S}T_{S}\sin\varphi = -V_{1}t_{1}\sin\frac{\pi}{3} - V_{2}t_{2}\sin\frac{\pi}{6} + V_{3}t_{3}\sin\frac{\pi}{3}$$
 (27)  
With the solution:

$$t_2 = \frac{\sqrt{2}V_S T_S}{V_{bat}} \cos\left(\varphi + \frac{\pi}{6}\right) \tag{28}$$

$$t_{1} = -t_{2} + T_{S} \left( \frac{1}{2} - \frac{\sqrt{2}V_{S}\sin\varphi}{V_{bat}} \right)$$
(29)  
$$t_{3} = T_{S} - t_{1} - t_{2}$$
(30)

 $t_3 = T_S - t_1 - t_2$ Sector 3 and 4  $(\frac{\pi}{3} < \varphi < \frac{4\pi}{3})$ 

The switching time equation is:

$$\vec{V}_S T_S = \vec{V}_1 t_1 + \vec{V}_3 t_3 + \vec{V}_4 t_4 \tag{31}$$

The vector decomposition of the above equation along Real and Imaginary axes in Figure 4:

$$T_{\rm S} = t_1 + t_3 + t_4 \tag{32}$$

Real: 
$$V_S T_S \cos \varphi = -V_1 t_1 \cos \frac{\pi}{3} + V_3 t_3 \cos \frac{\pi}{3} - V_4 t_4 \cos \frac{\pi}{6}$$
 (33)

*Imag*: 
$$V_S T_S \sin \varphi = -V_1 t_1 \sin \frac{\pi}{3} + V_3 t_3 \sin \frac{\pi}{3} + V_4 t_4 \sin \frac{\pi}{6}$$
 (34)

# 3. Simulation Results

The simulation is done by SIMULINK/MATLAB. The inverter is a full-bridge IGBT with extra switches that during the fault tolerant control, one leg (phase C) is connected to the middle point of a capacitor bank by one of the extra switches. The controller has a braking-chopper switch to control the bus voltage. Also it has a closed-loop (PI) speed regulation block. Electrical source is a 600Ah Lead-Acid battery. Its voltage, nominal discharge current and internal resistance is 650V, 600A and 10m $\Omega$  respectively. The motor is an induction three-phase squirrel-cage motor and its rated values and parameters are in Table 4.

Table 4 motor rated values and parameters

Power	15KW		
Voltage(line-line)	460V		
Frequency	60Hz		
Speed	1760rpm		
Pole pair(p)	2		
Rs	0.276Ω		
Rr	0.164Ω		
Ls	0.0021H		
Lr	0.0021H		
Lm	0.076H		
J	0.1Kg.m^2		
f	0.017N.m.s		

The system starts and runs normally in six-switch inverter algorithm with no load. It increases and regulates the speed to 1500RPM. The speed is regulated after t=0.75s (Figure 5). At t=1s, 40N.m load is connected to the motor. At t=1.25, the load is increased to full load 70N.m. At t=2s, the fault is occurred and the leg C is faulty (Figure 5). System continues to run by SVM sixswitch inverter algorithm. Figures 5 and 7, and Figures 5 and 10 show the stator current and electromagnetic torque are increased with distortion respectively. At t=2.2s, the modified SVM algorithm for four-switch inverter; operating in parallel before fault; is performed and connects the leg C to the middle point of a capacitor bank by send a signal command to the extra switch. Figures 5 and 8, and Figures 5 and 11 show the stator current and electromagnetic torque are reduced respectively and the distortion is reduced. Figure 6 is shown that speed regulation has ripple during t=2s and t=2.2s until the controller algorithm is changed to modified SVM algorithm for four-switch inverter. Bus voltage has ripple during the fault (t=2s to t=2.2s) (Figure 5). After t=2.5s motor speed is increased to 1760RPM by the modified SVM algorithm for four-switch inverter (Figure 5) that Figure 9 is shown that the stator current behavior is reasonable and it is reduced when the speed is regulated.



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Figure 8. Zoom around t=2.2s of Stator current(A) vs Time(second)



# 4. Conclusion

A low-cost fault tolerant control algorithm based on the SVM technique is presented. The algorithm and the related inverter-motor structure are simple and easy for practical implementation; in fact the algorithm does not require the motor modeling and parameters. The faulttolerant control includes two main algorithms; one for three-leg and the other for two-leg inverter; operating in parallel. In case a fault occurred on the inverter legs (open- or short-circuit) the algorithm changes-over on the mentioned algorithm.

The proposed control algorithm is verified by using a 15kW/460V/60Hz induction motor simulated with SIMULINK/MATLAB. The results obtain from simulation show stator current, electromagnetic torque and speed regulation behaviors reach desirable states by fault tolerant control. These states are very similar to six-switch inverter algorithm results without fault.

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## **Biographies**



Hamed Shahsavari Alavije was born in Tehran, Iran, on April 11, 1986. He received B.E.E and M.S.E.E degrees from Shahed University, Tehran, in 2008 and 2011.

His experiences are in analog circuit design, power electronic and motor drive. In 2007, he joined to Electrical Car Team (Rojan) in Amirkabir University of technology, where he worked on electronic circuit and motor control

His hobbies are reading book, making photoshop image, climbing, swimming and microstrip antenna design.

Mahdi Akhbari received the B.Sc. degree from Ferdowsi University of Mashad, Mashad, Iran, in 1993, the M.Sc. degree from Sharif University of Technology, Tehran, Iran, in 1995, and the Ph.D. degree from the Polytechnic of Grenoble, Grenoble, France in 2000, all with honors in electrical power engineering. Since 2000 he has been with the Department of Electrical Engineering at Shahed University, Tehran, Iran, where he is currently an Assistant professor. Dr. Akhbari's main research interests include modeling, analysis, design, and control of power electronic converters/systems and its application in Power system. In collaboration with industries and consulting engineering companies as technical advisor he has been involved in different applied researches; his experience encompasses conceptual design, detailed engineering and training in power system analysis, industrial power system rotection, protection coordination and power quality analysis.